

# Stretched-wire measurements of multipole magnets at the ESRF

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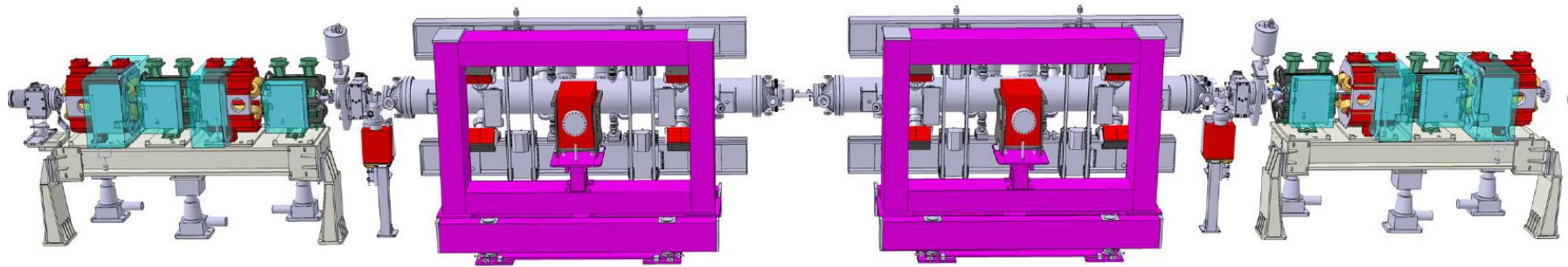
**Measurement bench**

**Results**

# Context

## ESRF Upgrade

- Longer straight sections : 5 m  $\rightarrow$  6 / 7m
- Lower vertical emittance, improved position diagnostics, etc.



Insertion devices straight section at the ESRF

## New Magnets

- Shorter quadrupoles and sextupoles
- Permanent Magnet steerers

# Introduction

## Stretched Wire Measurements

- Moving SW
- Vibrating SW (see next talks)

## Basic measurements

### Longitudinal field integral

$$I = \int B dl = -\frac{e}{v}$$

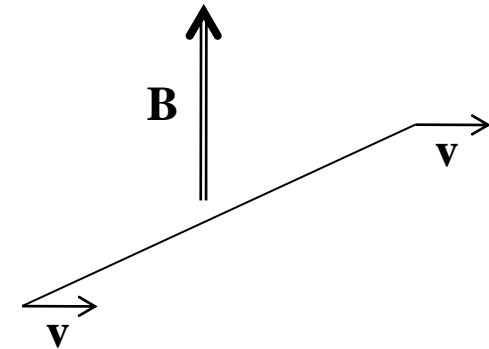
### Integration and time averaging

$$I = \frac{1}{L} \int e dt \qquad I \approx -\frac{\langle e \rangle T}{L}$$

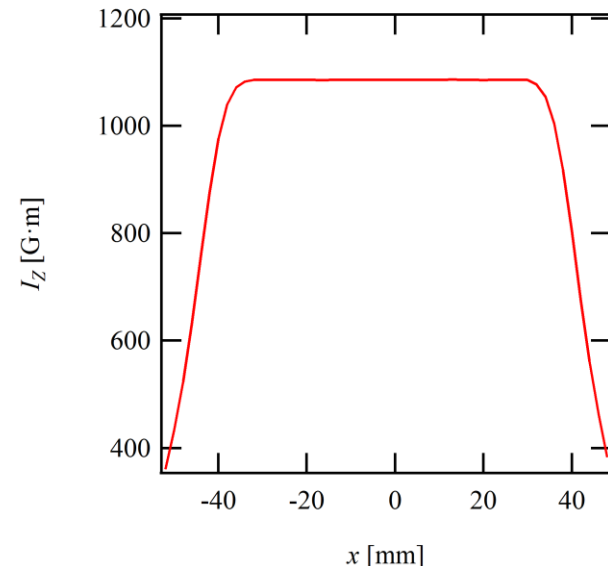
## Applications

Insertion devices

Field gradient, sextupole strength...



SW field integral measurement



PM Steerer field measurement

# Introduction

## Multipoles Analysis

### Complex potential

$$A = A + iV$$

### Multipole expansion

$$A = \sum_{n=0}^{\infty} c_n z^n$$

$$c_n = -\frac{b_n + i a_n}{n \rho_0^n}$$

## SW basic multipole measurements

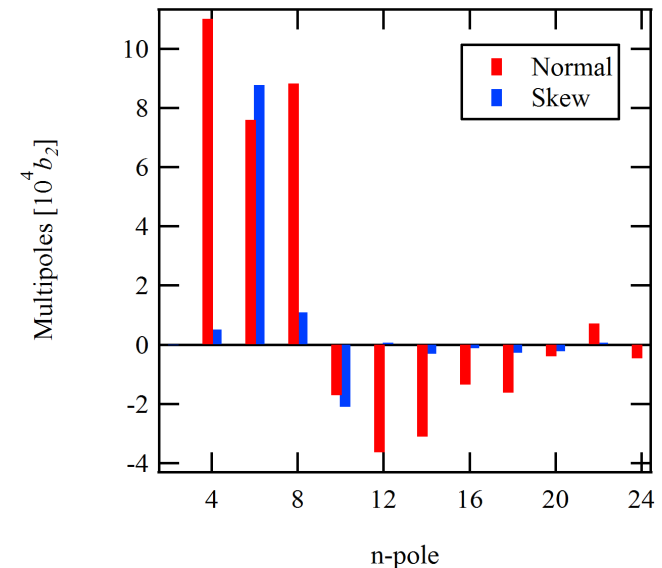
- Circular motion
- Fourier analysis
- Wire position errors
- No “bucking” available



**Low accuracy**

### Example

- ESRF Quadrupole
- Parasitic multipoles



**Basic SW quadrupole measurement**

# Theory

## Matrix formalism

Complex field integral

$$\mathbf{I}_{//\perp} = I_{\perp} + i I_{//} \quad \begin{array}{l} I_{\perp} \text{ is } \perp \text{ to the SW motion, measured} \\ I_{//} \text{ is } // \text{ to the SW motion, not measured} \end{array}$$

Can be written as

$$\mathbf{I}_{//\perp} = -e^{i\theta} (1, \dots, z^{n-1}) (\mathbf{c}_1, \dots, N \mathbf{c}_N)^T$$

For a set of measurements:

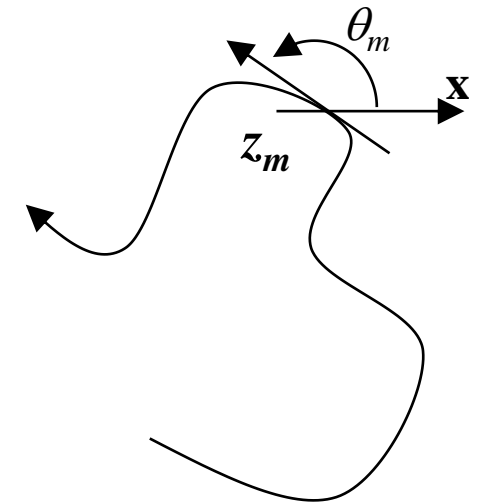
$$\begin{pmatrix} \mathbf{I}_{//\perp}^1 \\ \vdots \\ \mathbf{I}_{//\perp}^M \end{pmatrix} = \begin{pmatrix} e^{i\theta_1} & \dots & e^{i\theta_1} \left( \frac{\mathbf{z}_1}{\rho_0} \right)^{N-1} \\ \vdots & & \vdots \\ e^{i\theta_M} & \dots & e^{i\theta_M} \left( \frac{\mathbf{z}_M}{\rho_0} \right)^{N-1} \end{pmatrix} \begin{pmatrix} b_1 + i a_1 \\ \vdots \\ b_N + i a_N \end{pmatrix}$$



The measurements are expressed as:

$$\underbrace{(\mathbf{I}_{\perp}^1, \dots, \mathbf{I}_{\perp}^M)^T}_{\mathbf{I}} = \underbrace{(\text{Re } \mathbf{Z}, \text{Im } \mathbf{Z})}_{\mathbf{T}} \underbrace{(\dots, b_n, \dots, a_n, \dots)^T}_{\mathbf{C}}$$

with 
$$\mathbf{Z}_{mn} = e^{i\theta_m} \left( \frac{\mathbf{z}_m}{\rho_0} \right)^{n-1}$$



Arbitrary wire trajectory

# Theory

## Effect of measurement length

$$\mathbf{Z}_{mn} = \frac{1}{L} \int e^{i\theta_m} \left( \frac{z_m}{\rho_0} \right)^{n-1} dz$$

## Measured field integral

$\mathbf{I} = \mathbf{TC} \rightarrow$  Simulation from SW trajectory and multipoles

## Field multipoles

Least square inversion

$$\hat{\mathbf{C}} = (\mathbf{T}^T \mathbf{T})^{-1} \mathbf{T}^T \mathbf{I}$$

## Advantages

- Valid for any trajectory
- Position errors are taken into account

# Theory

## Multipole Compensation

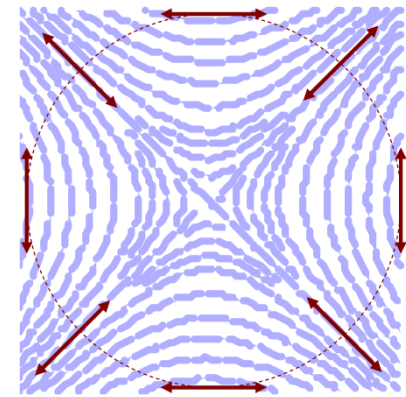
- SW parallel to the main multipole field lines
- Measurements at two radii at least



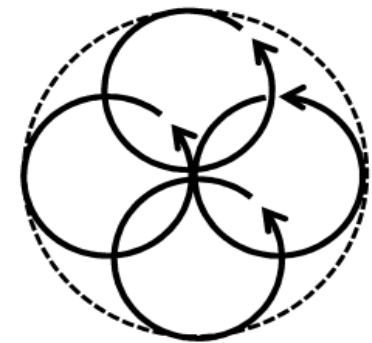
Similar to “bucked” coils

## Extension to rotating coils

- Simulation of coil errors
- Combining several rotating coil measurements



Compensation of the 4-pole



Multiple rotating coil measurements



# Accuracy

## Linear measurements

### Field Integral

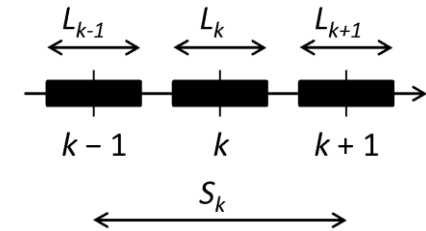
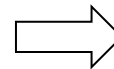
$$\frac{\Delta I}{I} = \frac{\Delta L}{L}$$

### Gradient

$$G_k^{meas} = \frac{I_{k+1}^{meas} - I_{k-1}^{meas}}{S_k}$$

$$= G_k + \Delta G_k$$

with  $|\Delta G_k| \leq \left| G_k \frac{\Delta S}{S} \right| + \frac{1}{S} \left| \frac{\Delta L}{L} \right| (|I_{k+1}| + |I_{k-1}|)$



Parameters for gradient calculations

**Field dependence**

# Accuracy

## Numerical simulations

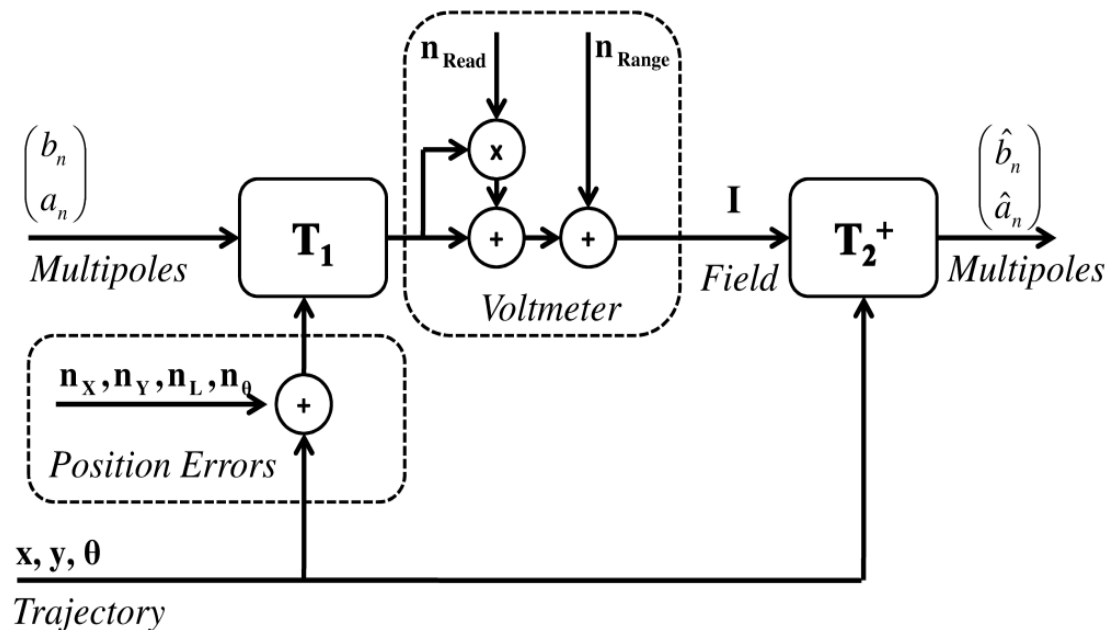
Multipoles and Trajectory



Several sample Fields and Estimated Multipoles

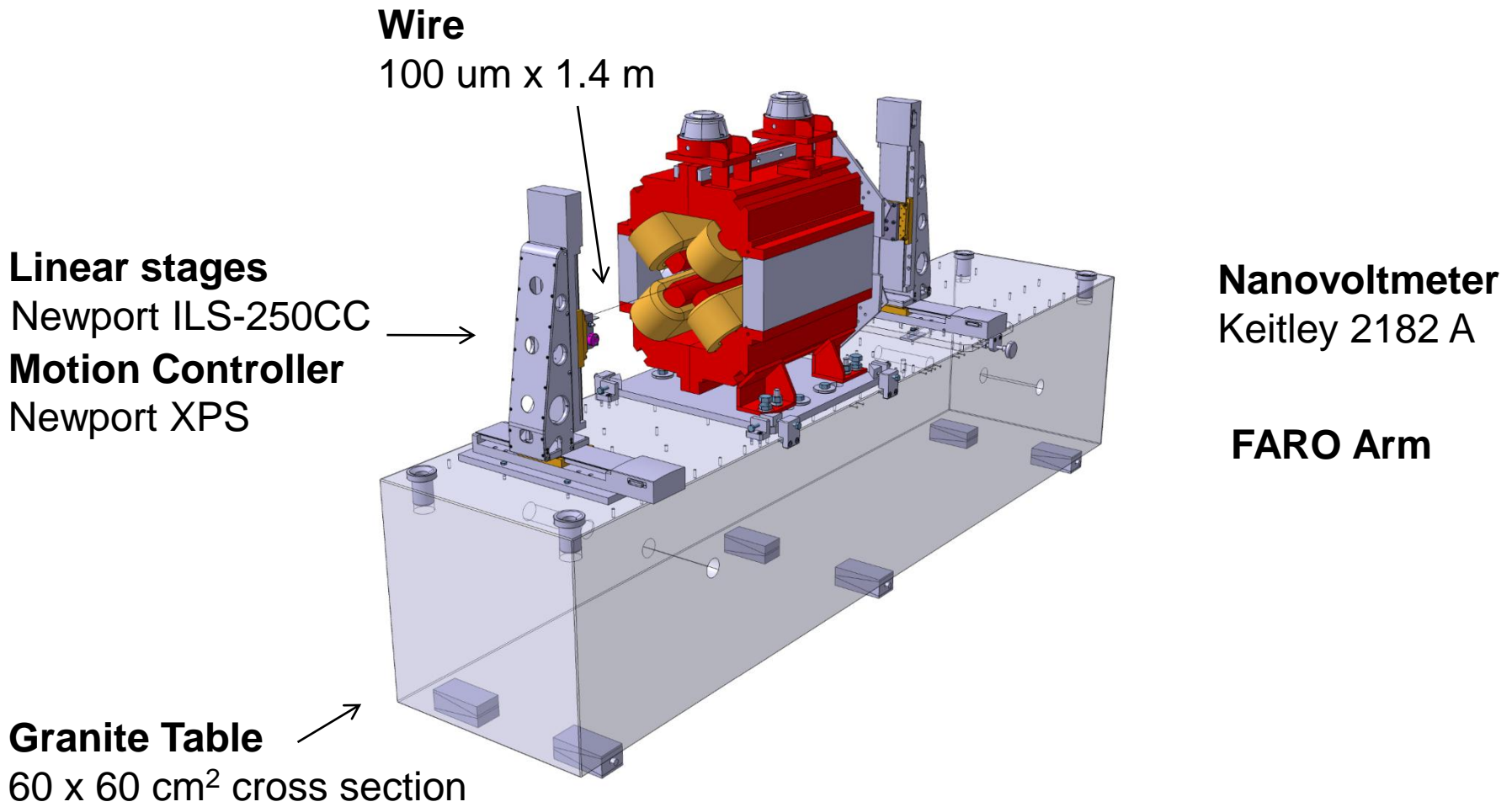


Sensitivities



Block diagram of the measurement model

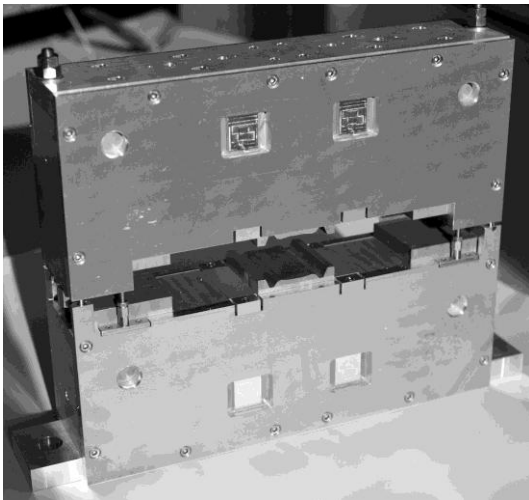
# Measurement bench



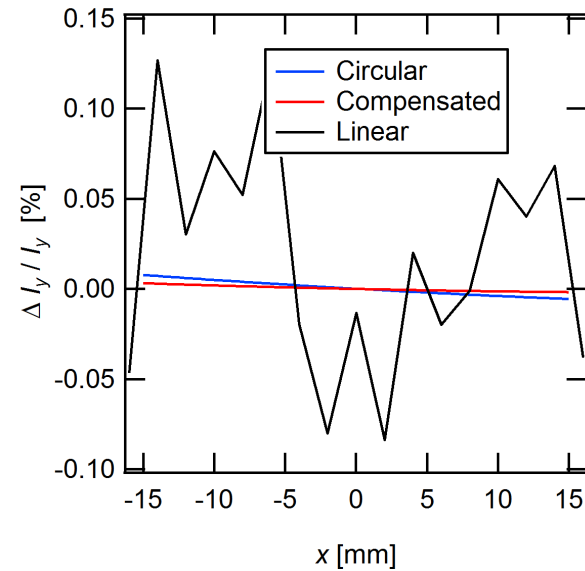
# Measurements

## Dipole

Max. field integral:  $5 \cdot 10^{-2}$  Tm



**PM Steerer**



**Dipole field measurements**

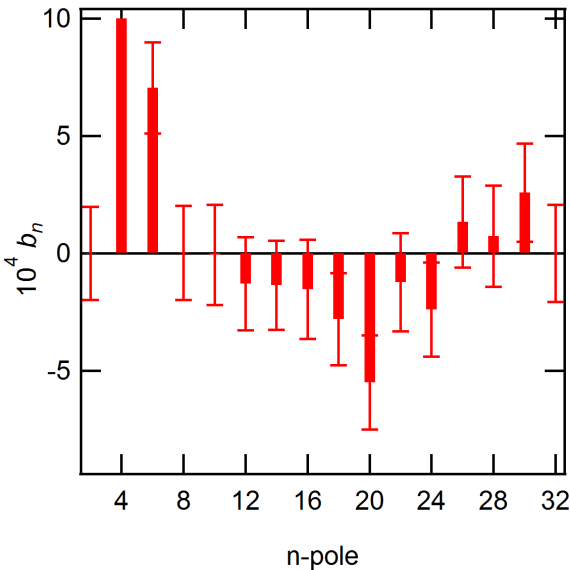
### Results

- Linear measurement → poor accuracy
- Multipole measurements are better

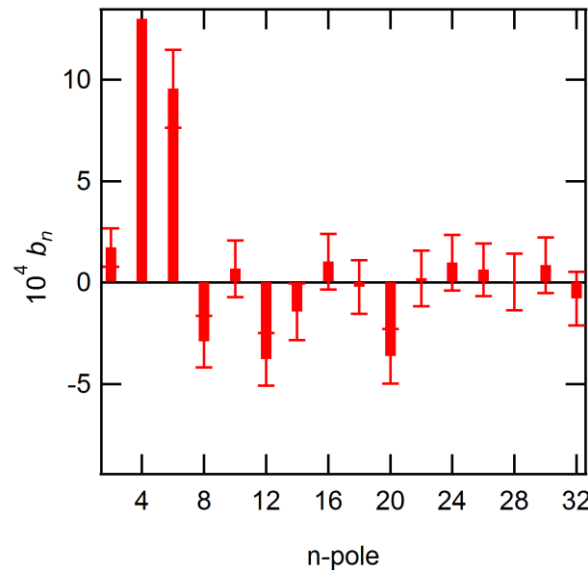
# Measurements

## Quadrupole

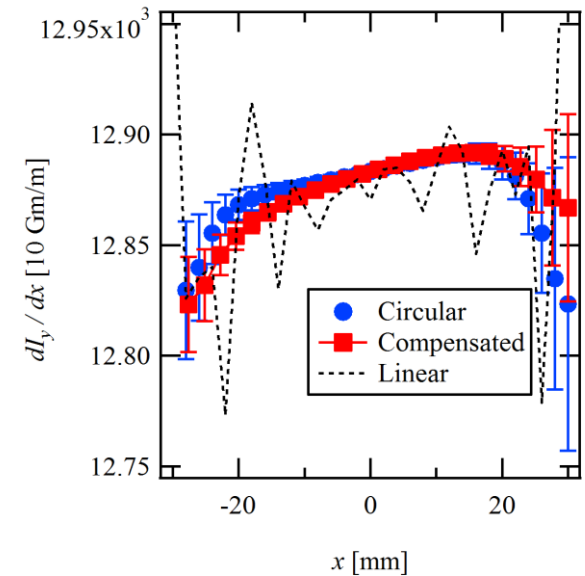
Gradient: 12.8 Tm/m; Max. field integral: 0.386 Tm



**Normal multipoles  
Circular trajectory**



**Normal multipoles  
Multipole compensated  
trajectory**



**Gradient**

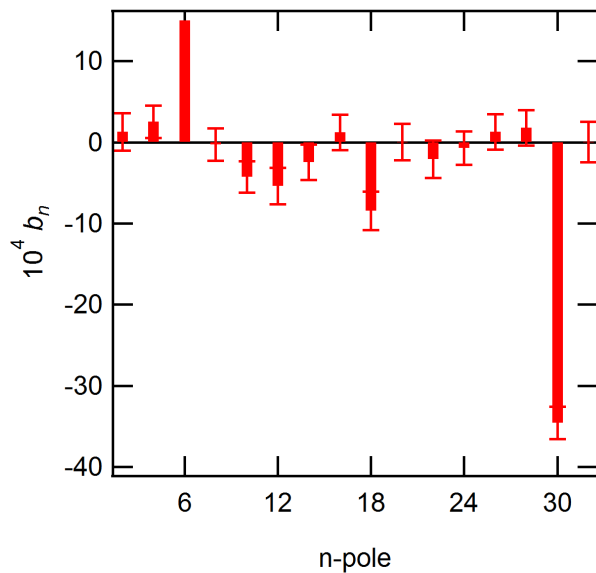
### Results:

- Multipole compensated trajectory gives better accuracy
- Poor accuracy of linear measurements

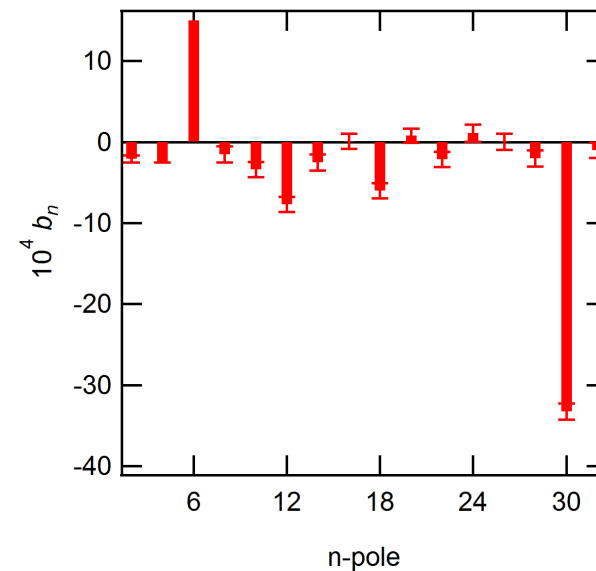
# Measurements

## Sextupole

Strength: 76.7 Tm/m<sup>2</sup>; Max. field integral: 3.45 10<sup>-2</sup> Tm



**Normal multipoles  
Circular trajectory**



**Normal multipoles  
Multipole compensated trajectory**

**Results:**

- Multipole compensated trajectory is better
- Circular trajectory gives acceptable accuracy

# Conclusion

## Theory

- Matrix formalism & least square approach
- Analysis of arbitrary trajectory
- SW “bucking” is available (compensated trajectories)
- Numerical simulations for sensitivity and accuracy analysis

## Measurements

- Linear measurements are not accurate
- Multipole compensated trajectories give the best results
- No reference magnet used

## Perspective

- Elliptic multipoles
- Non-circular trajectories